

## Early Journal Content on JSTOR, Free to Anyone in the World

This article is one of nearly 500,000 scholarly works digitized and made freely available to everyone in the world by JSTOR.

Known as the Early Journal Content, this set of works include research articles, news, letters, and other writings published in more than 200 of the oldest leading academic journals. The works date from the mid-seventeenth to the early twentieth centuries.

We encourage people to read and share the Early Journal Content openly and to tell others that this resource exists. People may post this content online or redistribute in any way for non-commercial purposes.

Read more about Early Journal Content at <a href="http://about.jstor.org/participate-jstor/individuals/early-journal-content">http://about.jstor.org/participate-jstor/individuals/early-journal-content</a>.

JSTOR is a digital library of academic journals, books, and primary source objects. JSTOR helps people discover, use, and build upon a wide range of content through a powerful research and teaching platform, and preserves this content for future generations. JSTOR is part of ITHAKA, a not-for-profit organization that also includes Ithaka S+R and Portico. For more information about JSTOR, please contact support@jstor.org.

79. Proposed by GEORGE LILLEY, Ph.D., LL. D., Professor of Mathematics, University of Oregon, Eugene, Oregon.

Find the area included between  $y=\sin^{\pi}x+\cos^{e}x$ ;  $y=\pi e(\sin^{\pi}x\cos^{e}x)$  and the length of its boundary, true to six decimal places, when  $\pi=3.14159$ , e=2.7182.

Solution by G. B. M. ZERR, A. M., Ph.D., Professor of Mathematics and Stience, Chester High School, Chester, Pa.

When  $x=0^{\circ}$ ,  $\sin^{\pi} x=0$ ,  $\cos^{e} x=1.0000$ .

When  $x=30^{\circ}$ ,  $\sin^{\pi} x=.1133$ ,  $\cos^{e} x=.6764$ .

When  $x=45^{\circ}$ ,  $\sin^{\pi} x = .3366$ ,  $\cos^{e} x = .3899$ .

When  $x=60^{\circ}$ ,  $\sin^{\pi} x = .8006$ ,  $\cos^{e} x = .1520$ .

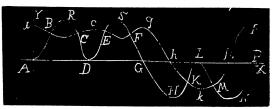
When  $x=90^{\circ}$ ,  $\sin^{\pi} x=1.0000$ ,  $\cos^{e} x=0$ .

Since e is even,  $\cos^e x$  is always positive; hence the following coördinates:

	$y = \sin^{\pi} x + \cos^{e} x$	$y = \pi e(\sin^{\pi} x \cos^{e} x)$
x	y	$\overline{y}$
$0^{\circ} = .0$	1.0000	0
$30^{\circ} = .5236$	.7897	.6541
$45^{\circ} = .7853$	.7265	1.1207
$60^{\circ} = 1.0471$	.9526	1.0392
$90^{\circ} = 1.5707$	1.0000	0
$120^{\circ} = 2.0942$	.9526	1.0392
$135^{\circ} = 2.3560$	.7265	1.1207
$150^{\circ} = 2.6178$	.7897	.6541
$180^{\circ} = 3.1414$	1.0000	0
$210^{\circ} = 3.6650$	.5631	6541
$225^{\circ} = 3.9268$	.0533	-1.1207
$240^{\circ} = 4.1886$	6480	-1.0392
$270^{\circ} = 4.7121$	-1.0000	0
$300^{\circ} = 5.2360$	6480	-1.0392
$315^{\circ} = 5.4978$	.0533	-1.1207
$330^{\circ} = 5.7596$	.5631	6541
$360^{\circ} = 6.2828$	1.0000	0

The curves drawn from these coördinates are somewhat like the figure, ABRCDESFGHKLMNP corresponding to  $y=\pi e(\sin^{\pi}x\cos^{e}x)$ ; aBCEFghKkMlp corresponding to  $y=\sin^{\pi}x+\cos^{e}x$ .

The curves are indefinite in length. The areas included between the curves from  $x=0^{\circ}$  to  $x=360^{\circ}$  are AaB+BRC+CDEc+ESF+FGHKhg+LMkK+PNMlp. The length of the boundary is



the whole length of both curves. The whole area common to both curves is infinite. The area above is but the area for one revolution. Area BRC=area ESF,

area AaB+ area PNMlp= area FGHKhg. The intersections are  $x=32^{\circ}48'$ ,  $x=61^{\circ}$ ,  $x=119^{\circ}$ ,  $x=147^{\circ}12'$ ,  $x=244^{\circ}22'$ ,  $x=295^{\circ}38'$ . The integrations are exceedingly tedious, but can be performed. If 3.1416 had been used for  $\pi$  the curves for one revolution would have consisted of four parts each equal to aBCc and ABRCD.

## MECHANICS.

Criticism on Professor Zerr's Solution of Problem 67, Mechanics, by J. M. ARNOLD, Crompton, R. I.

I wish to take exception to Professor Zerr's solution of No. 63 Mechanics, in the May number. The preliminary reasoning and the diagram are correct, but when he proceeds to find the required angles he commences with the assumption "The  $\angle ABC = \angle CDE$  and the  $\angle BAC = \angle \check{C}ED$ ." This is wrong as it can be easily shown that these angles are not equal. Therefore his result must be in error. I have not had time to solve the problem correctly, but I think it leads to very complicated equations.

## 70. Proposed by CHARLES E. MEYERS, Canton, Ohio.

A homogeneous sphere, radius r, having an angular velocity  $\omega$ , gradually contracts by cooling. What will be the angular velocity at the instant the radius becomes  $\frac{1}{2}r$ ?

Solution by WILLIAM HOOVER, A. M., Ph. D., Professor of Mathematics and Astronomy. Ohio University, Athens, Ohio.

Let m=the constant mass; r,  $\frac{1}{2}r$  the original and final radii;  $\omega'$ , the required angular velocity; k, k' the radii of gyration corresponding.

The moment of angular momentum remaining constant,

$$mk^2 \omega = mk'^2 \omega' \dots \dots (1).$$

But 
$$k^2 = \frac{1}{2}r^2$$
,  $k'^2 = \frac{1}{2}(\frac{1}{2}r)^2 = \frac{1}{8}r^2$ , (1) plainly gives  $\omega' = 4\omega$ .

Also solved in the same manner by G. B. M. ZERR.

## 71. Proposed by the late B. F. BURLESON, Oneida Castle, N. Y.

Three men own a sphere of gold the density of which varies as the square of the distance from the center. If two segments be cut off each one inch from the center of the sphere it will be divided into three parts of equal value. Determine the diameter of the sphere.

Solution by G. B. M. ZERR, A. M., Ph. D., Professor of Mathematics and Science, Chester High School, Chester Pa

Let  $\rho = \text{density} = r^2$  in this case, a = radius. Then the mass of each segment cut off is

$$\begin{split} M = & \int_{-1}^{a} \int_{-0}^{2\pi} \int_{0}^{\cos^{-1}(1/a)} \rho r^{2} \sin\theta d\theta d\varphi dr = & \int_{-1}^{a} \int_{0}^{2\pi} \int_{0}^{\cos^{-1}(1/a)} r^{4} \sin\theta dr d\varphi d\theta \\ &= \frac{2\pi}{5a} (a^{5} - 1)(a - 1). \end{split}$$